Are there any proofs (biblical and non-biblical) for existence of The Tower of Babel?

Legends, archeology and genealogies are consistent with the biblical account given in Genesis chapter 11 verses 1-4.

There are tower legends throughout the world which confirm an actual Tower of Babel.

There may be archeological evidence for the Tower of Babel, as well.

Bodie Hodge wrote:

In what is now Iraq, Robert Koldewey excavated a structure some think to be the foundation of the original Tower of Babel. It underlays a later ziggurat that was thought to be built by Hammurabi in the 19th century B.C.¹

Genealogies also reflect a common family.

Hodge continues:

...[G]enealogies seem to connect prominent modern houses and royal lines with the Table of Nations listed in the Bible. In these genealogies, Noah is found on the top of the lists on many of these documents, some of which feature variant spellings such as Noe, Noa, and Noah.²

Multiple languages are of course spoken all over the world. They appear to have originated from one language; perhaps, Hebrew.

God found it necessary to confuse things (Ge 11:1-32) as sinful men tried to unify themselves for their own glory (vv. 1-4). God had said to "Be fruitful and increase in number; fill the earth and subdue it (Ge 1:28)"; but, men chose instead to do opposite—stay close together and live as one. God then scattered them by confusing their language (vv. 5-9).

Men's plans were thwarted by God at that time (Gen. 11:5–9); but, evil men never gave up their aspirations. They have been trying to return to their Tower of Babel; and, in the end times they will achieve their goal of creating a one world government and religion (Re 13:1-18).

The Christian faith is an historical faith. Science does not disprove the bible; rather, time and time again it vindicates it.

¹ Hodge, Bodie. Was the Dispersion at Babel a Real Event? August 19, 2010: https://answersingenesis.org/towerof-babel/was-the-dispersion-at-babel-a-real-event/

² Ibid.